

Direction: Write neatly; show your work in an organized fashion.

1. Reduce:  $\frac{6x^2 + 17x + 7}{2x^2 + 7x + 3}$

2. Divide:  $\frac{25y^2 - 1}{9y^2 - 6y} \div \frac{5y^2 + 9y - 2}{3y^2 + y - 2}$

3. Add:  $\frac{x}{x^2 + 11x + 30} + \frac{-5}{x^2 + 9x + 20}$

4. Simplify:  $\frac{9 - \frac{1}{y^2}}{3 - \frac{1}{y}}$

5. Solve:  $\frac{7}{y} - \frac{1}{3} = \frac{1}{4}$

1. Reduce:  $\frac{6x^2 + 17x + 7}{2x^2 + 7x + 3} = \frac{(3x+7)(2x+1)}{(x+3)(2x+1)} = \frac{(3x+7)}{(x+3)}$

2. Divide:  $\frac{25y^2 - 1}{9y^2 - 6y} \div \frac{5y^2 + 9y - 2}{3y^2 + y - 2} = \frac{25y^2 - 1}{9y^2 - 6y} \cdot \frac{3y^2 + y - 2}{5y^2 + 9y - 2} = \frac{(5y+1)(5y-1)}{3y(3y-2)} \cdot \frac{(3y-2)(y+1)}{(5y-1)(y+2)}$

$$= \frac{(5y+1)(y+1)}{3y(y+2)}$$

3. Add:  $\frac{x}{x^2 + 11x + 30} + \frac{-5}{x^2 + 9x + 20} = \frac{x}{(x+5)(x+6)} + \frac{-5}{(x+4)(x+5)}$ , [ so LCD =  $(x+4)(x+5)(x+6)$  ]

$$= \frac{(x+4)x}{(x+4)(x+5)(x+6)} + \frac{-5(x+6)}{(x+4)(x+5)(x+6)} = \frac{x^2 + 4x}{(x+4)(x+5)(x+6)} + \frac{-5x - 30}{(x+4)(x+5)(x+6)} = \frac{x^2 + 4x - 5x - 30}{(x+4)(x+5)(x+6)}$$

$$= \frac{x^2 - x - 30}{(x+4)(x+5)(x+6)} = \frac{(x+5)(x-6)}{(x+4)(x+5)(x+6)} = \frac{(x-6)}{(x+4)(x+6)}$$

Multiply by a "fancy" one

4. Simplify:  $\frac{9 - \frac{1}{y^2}}{3 - \frac{1}{y}} = \frac{\left(9 - \frac{1}{y^2}\right) \left(\frac{y^2}{y^2}\right)}{\left(3 - \frac{1}{y}\right) \left(\frac{y^2}{y^2}\right)} = \frac{9y^2 - \frac{y^2}{y^2}}{3y^2 - \frac{y^2}{y}} = \frac{9y^2 - 1}{3y^2 - y} = \frac{(3y+1)(3y-1)}{y(3y-1)} = \frac{(3y+1)}{y}$

Multiply by "fancy" one and distribute  $y^2$  to all four terms

5. Solve:  $\frac{7}{y} - \frac{1}{3} = \frac{1}{4}$ . The LCM is  $12y$ , so multiply every term by  $12y$ .

$$\frac{12y \cdot 7}{y} - \frac{12y \cdot 1}{3} = \frac{12y \cdot 1}{4} \rightarrow 12 \cdot 7 - 4y \cdot 1 = 3y \cdot 1 \rightarrow 84 - 4y = 3y$$

$$\left. \begin{array}{l} 84 - 4y = 3y \\ +4y \quad +4y \end{array} \right\} \rightarrow \frac{84}{7} = \frac{7y}{7} \left. \right\} \rightarrow y = 12$$